

Deterministic and stochastic dynamics (MS327) content listing

Unit 1 <i>Introduction and differential equations</i>	Logistic equation, phase space, stability of fixed points, constants of motion, solving differential equations, separation of variables, complementary functions and particular integrals, integrating factor method
Unit 2 <i>Oscillations of linear systems</i>	Harmonic oscillator, coupled oscillators, normal modes, Lissajous curves, Fourier series, damped oscillators
Unit 3 <i>Nonlinear dynamics</i>	Phase flow, Lotka-Volterra equations, classification of equilibrium points, periodic solutions and limit cycles, Poincaré-Bendixson theorem, chaotic orbits, Lyapunov exponents
Unit 4 <i>Random motion and probability</i>	Random walk, probability density, uniform, normal and exponential distribution, mean value, variance, moments
Unit 5 <i>Introduction to the calculus of variations</i>	Functionals, stationary paths, Euler-Lagrange equations, first integral, Fermat's principle
Unit 6 <i>Lagrangian mechanics</i>	Kinetic and potential energy, Hamilton's principle, generalised coordinates, Lagrangian, action
Unit 7 <i>Exploring dynamics using maps</i>	Poincaré sections and return map, classification of fixed points, periodic orbits, logistic map, Hénon map
Unit 8 <i>Quantifying chaotic dynamics</i>	Lyapunov exponents, chaotic orbits, tent map, box-counting dimension, skinny baker's map, Kaplan-Yorke dimension
Unit 9 <i>Random walks and diffusion</i>	Concentration, flux, continuity equation, diffusion equation, Fick's law, advection-diffusion equation, Gauss's theorem, heat equation
Unit 10 <i>Fourier transforms</i>	Fourier transform, inverse Fourier transform, Fourier transform pairs, Fourier transform rules, convolution theorem
Unit 11 <i>Solving the diffusion equation</i>	Non-transform derivative rule, propagator, solving partial differential equations, Dirichlet and Neumann boundary conditions, eigenvalues and eigenfunctions, generalised Fourier series, Bessel functions
Unit 12 <i>Case studies in stochastic processes</i>	Absorbing and reflecting boundary conditions, survival probability, first passage probability, generalised random walks, Fokker-Planck equation, stationary probability density, Ornstein-Uhlenbeck process, applications in finance, Black-Scholes formulas